

For construction of parsing Table we need to find

FIRST

FOLLOW

FIRST

> In FIRST (1) we see Left Hand Side of the Production Rules.

> $\text{FIRST}(\epsilon) = \epsilon$
 $\text{FIRST}(\text{terminal}) = \text{terminal}$

> अगर ϵ आता है तो we have to remove it if it do not come directly. (2)

F

> In FOLLOW (1) we see Right Hand Side of the production rules.

> FOLLOW में ~~FIRST~~ भी आता है और FOLLOW भी आता है।

> अगर ϵ आता है (2) then we have to remove it.

> Follow of starting symbol always include \$

Q-2 Find FIRST and FOLLOW for the following Grammar.

$$S \rightarrow AaAb \quad - (i)$$

$$S \rightarrow BbBa \quad - (ii)$$

$$A \rightarrow \epsilon \quad - (iii)$$

$$B \rightarrow \epsilon \quad - (iv)$$

No ambiguity so
move further.

Sol:- First of all identify non-terminals

S, A, B

$$1. \text{ FIRST}(S) = \text{FIRST}(AaAb) \cup \text{FIRST}(BbBa) \quad (i, ii)$$

$$= \text{FIRST}(A) \cup \text{FIRST}(B)$$

we can't take

ϵ

$\cup$

ϵ

(iii, iv)

we can't take

$$\cancel{\epsilon} - \cancel{\epsilon} \cup \text{FIRST}(aAb) \cup \cancel{\epsilon} - \cancel{\epsilon} \cup \text{FIRST}(bBa)$$

a

$\cup$

b

{a, b}

3. $FIRST(B) = \{ \epsilon \}$. — we have to take as it comes directly.

FOLLOW

1. $FOLLOW(S) = \{ \$ \}$

2. $FOLLOW(A) = FIRST(aAb) \cup FIRST(b)$

$\{ a, b \}$

3. $FOLLOW(B) = FIRST(bBa) \cup FIRST(a)$

$(S(X) FIRST(b) \cup (b) FIRST(a))$

$\{ a, b \}$

$(a) FIRST(a) \cup (Y) FIRST(b) \cup b$

$(X) FIRST(b) \cup a \cup b$

$FOLLOW(S) = \{ \$ \}$

whose FIRST and FOLLOW sets
 grammar productions are given

Start symbol (Z)

$$Z \rightarrow d \quad - (i)$$

$$Z \rightarrow XYZ \quad - (ii)$$

$$Y \rightarrow \epsilon \quad - (iii)$$

$$Y \rightarrow c \quad - (iv)$$

$$X \rightarrow Y \quad - (v)$$

$$X \rightarrow a \quad - (vi)$$

Sol:-

Non-terminals $\{d, c\}$

X, Y, Z

Imp

$$1. \boxed{\text{FIRST}(Z)} =$$

$$\text{FIRST}(d) \cup \text{FIRST}(X \overset{\vee}{Y} \hat{Z})$$

$$d \cup \text{FIRST}(X)$$

$$d \cup \text{FIRST}(Y) \cup \text{FIRST}(a)$$

$$d \cup a \cup \text{FIRST}(Y)$$

FIRST(Y)
 $\{c, \epsilon\}$

$$d \cup a \cup c \cup \epsilon - \epsilon \cup \text{FIRST}(z)$$

$$\boxed{\{a, c, d\} \cup \text{FIRST}(z)}$$

we don't have to go further as we are finding FIRST(z) and getting FIRST(z) i Union.

no need.

$$\times \{a, c, d\} \cup \text{FIRST}(d) \cup \text{FIRST}(xyz)$$

$$\{a, c, d\} \cup \text{FIRST}(z)$$

$$\text{Ans} \{b, c, d\} =$$

$$= \{a, c, d\} \text{ Ans.}$$

FIRST

Follow (X) =

$$2. \text{FIRST}(Y) = \text{FIRST}(c) \cup \epsilon$$

$$= \{c, \epsilon\} \text{ Ans.}$$

we can't delete ϵ as it comes directly.

Imp

$$3. \boxed{\text{FIRST}(X)} =$$

$$\text{FIRST}(Y) \cup \text{FIRST}(a)$$

$$= \{c, \epsilon\} \cup a$$

$$= \{a, c, \epsilon\} \text{ Ans.}$$

$$1. \text{ FOLLOW}(Z) = \{\$ \} \text{ Ans.}$$

as in R.H.S of production rules there is no symbol following X so it follow X

$$\begin{aligned} 2. \text{ FOLLOW}(Y) &= \text{FIRST}(Z) \cup \text{FOLLOW}(X) \\ &= \{a, c, d\} \cup \{a, c, d\} \\ &= \{a, c, d\} \cup \{a, c, d\} \\ &= \{a, c, d\} \text{ Ans.} \end{aligned}$$

$$\begin{aligned} 3. \text{ FOLLOW}(X) &= \text{FIRST}(YZ) \\ &= \text{FIRST}(Y) \\ &= \{c, \epsilon\} - \epsilon \cup \text{FOLLOW}(X) \cup \text{FIRST}(Z) \\ &= \{c, \epsilon\} - \epsilon \cup \text{FOLLOW}(X) \cup \{a, c, d\} \\ &= \{a, c, d\} \text{ Ans.} \end{aligned}$$

we can't take ϵ so check for ϵ

FOLLOW(Y)

(a) FIRST(Y) FIRST(Z)

= (X) FIRST(Z)

part (c)

$$E \rightarrow TE'$$

$$E' \rightarrow +TE' \mid \epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT' \mid \epsilon$$

$$F \rightarrow (E) \mid id$$

Sol:-

Non terminals are

E, E', T, T', F

WOLLOF

FIRST

$$\begin{aligned} 1. \text{ FIRST}(E) &= \text{FIRST}(TE') \\ &= \text{FIRST}(T) \\ &= \text{FIRST}(FT') \\ &= \text{FIRST}(F) \\ &= \text{FIRST}((E)) \cup \text{FIRST}(id) \\ &= (\cup id \end{aligned}$$

$$= \{ (, id \} \text{ Ans.}$$

$$\begin{aligned} 2. \text{ FIRST}(E') &= \text{FIRST}(+TE') \cup \epsilon \\ &= \text{FIRST}(+) \cup \epsilon \\ &= \{ +, \epsilon \} \text{ Ans.} \end{aligned}$$

$$\begin{aligned}
 4. \text{ FIRST}(T') &= \text{FIRST}(*FT') \cup \epsilon \\
 &= \text{FIRST}(*) \cup \epsilon \\
 &= \{*, \epsilon\} \text{ Ans.}
 \end{aligned}$$

$$5. \text{ FIRST}(F) = \{c, id\} \text{ Ans.}$$

FOLLOW

$$\begin{aligned}
 1. \text{ FOLLOW}(E) &= \text{FIRST}()) \cup \{\$ \} \\
 &= \{), \$\} \text{ Ans.}
 \end{aligned}$$

$$\begin{aligned}
 2. \text{ FOLLOW}(E') &= \text{FOLLOW}(E) \\
 &= \{), \$\} \text{ Ans.}
 \end{aligned}$$

$$\begin{aligned}
 3. \text{ FOLLOW}(T) &= \text{FIRST}(E') \cup \text{FOLLOW}(E) \\
 &= \{+, \epsilon\} \cup \{), \$\} \text{ Ans.}
 \end{aligned}$$

we can't take ϵ so use

$\text{FOLLOW}(E')$

$$4. \text{ FOLLOW}(T') = \text{ FOLLOW}(T) \\ = \{ +,), \$ \} \text{ Ans.}$$

$$5. \text{ FOLLOW}(F) = \text{ FIRST}(T') \\ = \{ *, \epsilon \} - \epsilon \cup \text{ FOLLOW}(T) \\ = \{ *, +,), \$ \} \text{ Ans.}$$

$$\begin{aligned} T &\rightarrow (E) \quad \text{--- (i)} \\ T &\rightarrow *FT \quad \text{--- (ii)} \\ T &\rightarrow FT \quad \text{--- (iii)} \\ T &\rightarrow +TE \quad \text{--- (iv)} \\ E &\rightarrow TE \end{aligned}$$

Sol:- The non-terminals are E, F, T, T'

and

$$\begin{aligned} \text{FIRST}(T) &= \{ *, \epsilon \} \\ \text{FIRST}(E) &= \{ +, \epsilon \} \\ \text{FIRST}(F) &= \{ \epsilon, + \} \end{aligned}$$

$$\begin{aligned} \text{FOLLOW}(T) &= \{ +,), \$ \} \\ \text{FOLLOW}(E) &= \{ +,), \$ \} \\ \text{FOLLOW}(F) &= \{ +,), \$ \} \end{aligned}$$

Construction of Predictive Parsing Table

Grammar:-

Q → Construct the parsing Table for the
whose productions are given:-

$$E \rightarrow TE' \quad \text{--- (i)}$$

$$E' \rightarrow +TE' / \epsilon \quad \text{--- (ii)}$$

$$T \rightarrow FT' \quad \text{--- (iii)}$$

$$T' \rightarrow *FT' / \epsilon \quad \text{--- (iv)}$$

$$F \rightarrow (E) / id. \quad \text{--- (v)}$$

Sol:- The non-terminals are

E, E', T, T', F

and

$$FIRST(E) = \{ (, id \} = FIRST(T) = FIRST(F)$$

$$FIRST(E') = \{ +, \epsilon \}$$

$$FIRST(T') = \{ *, \epsilon \}$$

$$FOLLOW(E) = \{), \$ \} = FOLLOW(E')$$

$$FOLLOW(T) = \{ +,), \$ \} = FOLLOW(T')$$

$$FOLLOW(F) = \{ *, +,), \$ \}.$$

Non Terminals	id	+	*	(	)	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$		$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$	
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$	$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$	
F	$F \rightarrow id$			$F \rightarrow (E)$		

$\{ (, + \} = (T) FIRST +$

$\{ (, + \} = (blank boxes are errors.$

$\{ (, + \} = (T) FIRST$

(check where

$FIRST (non terminal) = ((, +)$
 $FOLLOW (non terminal) = (), $$

1. For E

$FIRST(E) = \{ (, id \}$

/* both terminals
 So directly write the production rule of E in table */

2. For E'

$FIRST(E') = \{ +, (\}$

$FOLLOW(E') = \{), $ \}$

/* one is terminal one is null
 So check FOLLOW E' */
 $E' \rightarrow \epsilon$ वाला rule) में आसगा
 $E' \rightarrow +TE'$ वाला rule + में आसगा

$$4 \text{ FIRST}(T') = \{ *, (\}$$

$$\text{FOLLOW}(T') = \{ +,), \$ \}$$

$$5 \text{ FIRST}(F) = \{ (, id \}$$

/* Both are terminals

(comes from $F \rightarrow (E)$

id comes from $F \rightarrow id$

For entries of \$ attribute

Check where

$$\text{FIRST}(\text{non Terminal}) = ($$

$$\text{FOLLOW}(\text{non Terminal}) = \$$$

$$\text{add } E' \rightarrow ($$

$$T' \rightarrow ($$

\$ attribute

Type 0 (Recursive Enumerate grammar or Unrestricted grammar)

Type 1 (CSG or Context Dependent Grammar)

Type 2 (CFG or Context Independent Grammar or Phrase Structured)

(Nesting of
parenthesis

Type 3 (Regular grammar)

Type 0

Every production is in the form

$$(V+T)^* \longrightarrow (V+T)^*$$

But remember the basic rule that in every production rule
Atleast one Non Terminal must be there in LHS

e.g

$$S \rightarrow aABb$$

$$aA \rightarrow bBa/b$$

$$Bb \rightarrow aB / Bab/a$$

Type 1

Every Production Rule is in the form

$$(V+T)^* \longrightarrow (V+T)^*$$

+

2 more conditions

(i) $|LHS| \leq |RHS|$

(ii) $RHS \neq \epsilon$

* But remember the basic rule that in every production rule
Atleast one Non Terminal must be there in L.H.S

e.g

$$S \longrightarrow aSAc/abc$$

$$cA \longrightarrow Ab$$

$$bA \longrightarrow bb$$

Some Imp Points about Type 1

Type 1 grammar is also called as length increasing grammar because

The language generated by Type 1 grammar is free from ϵ .

Every Production Rule is in the form

एक variable $\rightarrow (V+T)^*$

e.g

$S \rightarrow aSc \mid aAc$

$A \rightarrow ab \mid \epsilon$

Some Imp points about Type 2

All programming languages are defined by Type 2 grammar
All compilers understand Type 2 grammar
and parsers (LR(k) e.t.c)

Type - 3

Every production Rule is in the form

एक variable $\rightarrow$ एक या एक से अधिक terminals

या

एक variable $\rightarrow \epsilon$

या इन दोनों में से एक

Left Linear

एक variable $\rightarrow$ एक variable. एक या एक से अधिक terminals

एक variable $\rightarrow$ एक या एक से अधिक terminals. एक variable

Right Linear

Ardens Theorem

The Regular Expression of DFA, NFA is found with the help of Ardens theorem.

Drawback:- Ardens theorem cannot be used with ϵ -transition
(i.e. cannot be used with ϵ -NFA)

Ardens Theorem :- eq of each state according to inside arrow to the state

$$Y = mY + c$$

initial state के साथ ϵ add करना है

only terminals

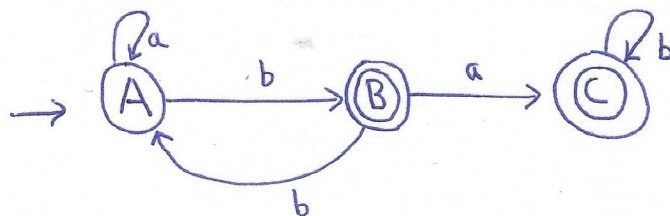
then RE for the state is

$$Y = cm^*$$

If final states are more than one

R.E for given $m/c =$ R.E one final state + R.E 2nd final state + ...

Q →



$$R.E \text{ of } m/c = R.E_B + R.E_C$$

$$A = Aa + Bb + \epsilon$$

$$B = Ab$$

$$C = Cb + Ba$$

$$A = Aa + Bb + \epsilon$$

$$= Aa + Abb + \epsilon$$

$$A = A(a+bb) + \epsilon$$

$$R.E = \epsilon(a+bb)^* = (a+bb)^*$$

$$B = Ab$$

$$= (a+bb)^*b$$

$$C = Cb + \frac{(a+bb)^*ba}{s}$$

$$R.E = (a+bb)^*bab^*$$

$$R.E_{m/c} = R.E_B + R.E_C$$

$$= (a+bb)^*b + (a+bb)^*bab^*$$

$$R.E_{m/c} = (a+bb)^*b + (a+bb)^*bab^*$$